

# SOLUTIONS

## MOCK EXAMINATION 5

### Paper 1

#### Booklet A

1 (3)

$$(1) \frac{1}{3} = 0.3333$$

$$(2) \frac{2}{5} = 0.4$$

$$(3) 30\% = 0.3 \rightarrow \text{smallest}$$

$$(4) 0.45$$

2 (2)

$$100 \text{ tens} \rightarrow 1000$$

$$20 \text{ hundredths} = \frac{20}{100} = 0.2$$

$$1000 - 0.2 = \mathbf{999.8}$$

3 (3)

$$\frac{3}{12} = \frac{2}{\square}$$

$$\frac{3 (\times 2)}{12 (\times 2)} = \frac{6}{24}$$

$$\frac{6 (\div 3)}{24 (\div 3)} = \frac{2}{8}$$

$$\square \rightarrow 8$$

4 (2)

$$1 \times 6 = 6$$

$$2 \times 3 = 6$$

Factors of 6  $\rightarrow$  1, 2, 3, 6

$$1 \times 18 = 18$$

$$2 \times 9 = 18$$

$$3 \times 6 = 18$$

Factors of 18  $\rightarrow$  1, 2, 3, 6, 9, 18

Common factors of 6 and 18  $\rightarrow$  **2 and 3**

5 (3)

$$2\frac{1}{4} \text{ kg} = 2.25 \text{ kg} = 2250 \text{ g}$$

$$\frac{450 \text{ g}}{2250 \text{ g}} \times 100\% = \mathbf{20\%}$$

6 (4)

Area of a face of a cube  $\rightarrow$  length  $\times$  length

$$49 \text{ cm}^2 \rightarrow 7 \text{ cm} \times 7 \text{ cm}$$

Since it is a cube, all the lengths are the same.

Volume of a cube  $\rightarrow$  length  $\times$  length  $\times$  length

$$\rightarrow 7 \text{ cm} \times 7 \text{ cm} \times 7 \text{ cm}$$

$$= 343 \text{ cm}^3$$

Volume of 2 cubes  $\rightarrow 343 \text{ cm}^3 \times 2$

$$= \mathbf{686 \text{ cm}^3}$$

7 (4)

Clarice : Serene : Zoe

$$3 (\times 5) : 4 (\times 5)$$

$$15 (\times 3) : \quad \quad \quad 1 (\times 3)$$

$$\mathbf{15 : 20 : 3}$$

8 (2)

Fraction of water in the container  $\rightarrow \frac{2}{5}$  (2 units)

Fraction of water needed to fill to its brim

$$\rightarrow 1 - \frac{2}{5} = \frac{3}{5} \text{ (3 units)}$$

Volume of water poured to its brim  $\rightarrow 258 \text{ m}\ell$

$$3 \text{ units} = 258 \text{ m}\ell$$

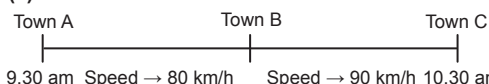
$$1 \text{ unit} = 258 \text{ m}\ell \div 3$$

$$= 86 \text{ m}\ell$$

Volume of water at first  $\rightarrow 86 \text{ m}\ell \times 2 \text{ units}$

$$= \mathbf{172 \text{ m}\ell}$$

9 (4)



9:30 am Speed  $\rightarrow$  80 km/h Speed  $\rightarrow$  90 km/h 10:30 am

Time taken from Town A to Town C  $\rightarrow$  1 h

Since the whole journey took 1 h and the speed is calculated on a per hour basis, we can add the speed together for 2 hours.

Speed  $\rightarrow$  80 km/h + 90 km/h

$$\rightarrow 170 \text{ km in 2 hours}$$

2 hours  $\rightarrow$  170 km

1 hour  $\rightarrow$  170 km  $\div$  2 hours

$$= 85 \text{ km}$$

Therefore, he travelled at an average speed of **85 km/h**.

10 (4)

Fraction of beads remaining  $\rightarrow 1 - \frac{2}{5} = \frac{3}{5}$

Fraction of beads Amy had left  $\rightarrow$  80% of remainder

$$= \frac{80}{100} \times \frac{3}{5}$$

$$= \frac{12}{25} \text{ (12 units)}$$

Number of beads Amy had left  $\rightarrow$  120

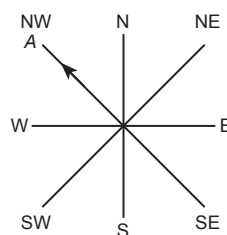
$$12 \text{ units} = 120$$

$$1 \text{ unit} = 120 \div 12 = 10$$

Number of beads Amy had at first  $\rightarrow 10 \times 25 \text{ units}$

$$= \mathbf{250}$$

11 (3)



Thomas is facing north-west.

$$\frac{1}{8} - \text{turn} \rightarrow 45^\circ$$

$$\frac{3}{8} - \text{turn} \rightarrow 45^\circ \times 3 = 135^\circ$$

Since Thomas made a  $135^\circ$  turn in the clockwise direction, we will reverse in the anti-clockwise direction to find where he was at first.

From NW to SW  
 → 90° anti-clockwise direction  
 From SW to S  
 → 45° anti-clockwise direction

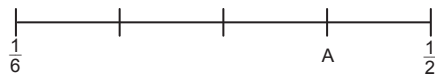
} 90° + 45° = 135°

Therefore, Thomas was facing **South** at first.

12 (4)

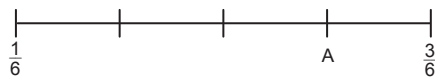
Amount of money Mrs Sim spent last month → \$720  
 Percentage of money Mrs Sim spent this month  
 → increased by 20%  
 → 100% + 20%  
 = 120%  
 Amount of money Mrs Sim spent this month  
 →  $\frac{120}{100} \times \$720$   
 = \$864  
 Total amount of money Mrs Sim spent in 2 months  
 → \$720 + \$864  
 = **\$1584**

13 (2)



First, we will make the denominator for  $\frac{1}{2}$  to 6 (same as the denominator for  $\frac{1}{6}$ )

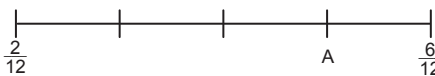
$$\frac{1 \times 3}{2 \times 3} = \frac{3}{6}$$



There are 4 units from  $\frac{1}{6}$  to  $\frac{3}{6}$ , we cannot determine the actual fraction for 'A' as the difference in their numerators is quite narrow. Therefore, we will multiply by 2 to their numerators and denominators for both  $\frac{1}{6}$  and  $\frac{1}{2}$  to check if we can find the fraction for each unit.

$$\frac{3 \times 2}{6 \times 2} = \frac{6}{12}$$

$$\frac{1 \times 2}{6 \times 2} = \frac{2}{12}$$



Now, we can see that from  $\frac{2}{12}$  to  $\frac{6}{12}$ , the difference is  $\frac{4}{12}$ . We can conclude that each unit is  $\frac{1}{12}$  for the 4 units above and the fraction is increasing. Therefore, the fraction that represents A →  $\frac{5}{12}$

14 (3)

Mass of grapes Timothy bought →  $\frac{1}{4}$  kg  
 Mass of grapes Timothy ate →  $\frac{1}{6}$  of them  
 →  $\frac{1}{6} \times \frac{1}{4}$  kg  
 =  $\frac{1}{24}$  kg

Mass of grapes Timothy had left →  $\frac{1}{4}$  kg -  $\frac{1}{24}$  kg  
 =  $\frac{1 \times 6}{4 \times 6}$  kg -  $\frac{1}{24}$  kg  
 =  $\frac{6}{24}$  kg -  $\frac{1}{24}$  kg  
 =  $\frac{5}{24}$  kg

Number of bags → 5  
 Mass of each bag of grapes →  $\frac{5}{24}$  kg ÷ 5  
 =  $\frac{5}{24}$  kg ×  $\frac{1}{5}$   
 =  $\frac{1}{24}$  kg

15 (3)

Percentage of children → 60%  
 Percentage of adults → 100% - 60% = 40%  
 Percentage of men → 30% of the adults  
 Percentage of women  
 → (100% - 30%) of the adults  
 = 70% of the adults  
 =  $\frac{70}{100} \times 40\%$   
 = 28%

Total number of people at the carnival → 250  
 Number of women at the carnival → 28% × 250  
 =  $\frac{28}{100} \times 250$   
 = **70**

**Booklet B**

16 Eighths →  $\frac{1}{8}$

$$5\frac{3}{4} \div \frac{1}{8} = \frac{23}{4} \times \frac{8}{1}$$

$$= \frac{184}{4}$$

$$= **46**$$

17  $2.24 \times 6 = 134.4 \times \square$

$$13.44 = 134.4 \div 10$$

$$= 134.4 \div \frac{10}{1}$$

$$= 134.4 \times \frac{1}{10}$$

$$\square \rightarrow \frac{1}{10} = **0.1**$$

**Alternative method:**

$2.24 \times 6 = 134.4 \times \square$

$$\square = \frac{2.24 \times 6}{134.4}$$

$$= \frac{13.44}{134.4}$$

$$= **\frac{1}{10}**$$

18 1st 2nd 3rd 4th 5th 6th 7th 8th 9th 10th 11th 12th 13th  
 { 2nd to 5th }  
 21 m

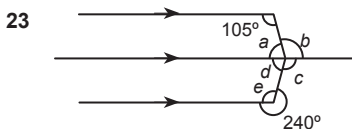
Number of intervals (units) between 2nd and 5th trees  
 → 3  
 3 units = 21 m  
 1 unit = 21 m ÷ 3 = 7 m  
 Number of intervals (units) between 3rd and 13th tree  
 → 10  
 10 units = 7 m × 10 = **70 m**

- 19 Amount Clarice spent on 100 g of grapes on Monday → \$2.50  
 Mass of grapes she bought on Tuesday → 2 kg = 2000 g  
 100 g → \$2.50  
 $2000 \text{ g} \rightarrow \frac{2000}{100} \times \$2.50$   
 $= \$50$   
 Total amount of money Clarice spent on Monday and Tuesday → \$2.50 + \$50  
 $= \$52.50$

- 20 Ratio of breadth to length of rectangle → 2 : 3  
 Number of units representing perimeter of the rectangle  
 →  $(2 \times \text{length}) + (2 \times \text{breadth})$   
 →  $(2 \times 3 \text{ units}) + (2 \times 2 \text{ units})$   
 $= 6 \text{ units} + 4 \text{ units}$   
 $= 10 \text{ units}$   
 10 units = 130 cm  
 1 unit =  $130 \text{ cm} \div 10$   
 $= 13 \text{ cm}$   
 Length of rectangle →  $13 \text{ cm} \times 3$   
 $= 39 \text{ cm}$

- 21 Radius of semicircle → 14 cm  
 Diameter of semicircle →  $14 \text{ cm} \times 2 = 28 \text{ cm}$   
 Circumference of semicircle →  $\frac{1}{2} \times 2\pi r$   
 $\rightarrow \frac{1}{2} \times 2 \times \frac{22}{7} \times 14 \text{ cm}$   
 $= \frac{616}{14} \text{ cm}$   
 $= 44 \text{ cm}$   
 Perimeter of semicircle → circumference + diameter  
 $\rightarrow 44 \text{ cm} + 28 \text{ cm}$   
 $= 72 \text{ cm}$

- 22 Length of tank → 3 m = 300 cm  
 Number of 3-cm lengths to fit length of tank  
 $\rightarrow 300 \text{ cm} \div 3 \text{ cm} = 100$   
 Width of tank → 5 m = 500 cm  
 Number of 3-cm widths to fit width of tank  
 $\rightarrow 500 \text{ cm} \div 3 \text{ cm}$   
 $= 166 \text{ R } 2$   
 $\approx 166$  (Round down)  
 Height of tank → 6 m = 600 cm  
 Number of 3-cm heights to fit height of tank  
 $\rightarrow 600 \text{ cm} \div 3 \text{ cm}$   
 $= 200$   
 Maximum number of 3-cm cubes to fit into the tank  
 $\rightarrow 100 \times 166 \times 200$   
 $= 3\ 320\ 000$



- We divide the figure into half.  
 $\angle a = 180^\circ - 105^\circ$  (angles between two parallel lines)  
 $= 75^\circ$   
 $\angle b = 180^\circ - 75^\circ$  (angles on a straight line)  
 $= 105^\circ$

- $\angle e = 360^\circ - 240^\circ = 120^\circ$  (angles at a point)  
 $\angle d = 180^\circ - 120^\circ$  (angles between two parallel lines)  
 $= 60^\circ$   
 $\angle c = 180^\circ - 60^\circ$  (angles on a straight line)  
 $= 120^\circ$   
 $\angle y = \angle b + \angle c$   
 $= 105^\circ + 120^\circ$   
 $= 225^\circ$

- 24  $5\text{¢} \times 21 \text{ coins} = \$1.05$   
 $10\text{¢} \times 50 \text{ coins} = \$5.00$   
 $20\text{¢} \times 22 \text{ coins} = \$4.40$   
 $50\text{¢} \times 15 \text{ coins} = \$7.50$   
 $\$1 \times 6 \text{ coins} = \$6.00$   
 Total amount of money Ray has saved  
 $\rightarrow \$1.05 + \$5.00 + \$4.40 + \$7.50 + \$6.00 = \$23.95$

- 25 Each row represents 2 seashells.  
 Mandy, Candy and Sandy collected 12 seashells each.  
 Number of seashells Timmy collected → 24  
 Number of seashells Timmy collected more than each of his friends →  $24 - 12 = 12$   
 Number of seashells Timmy must give each of his friends →  $12 \div 4 = 3$

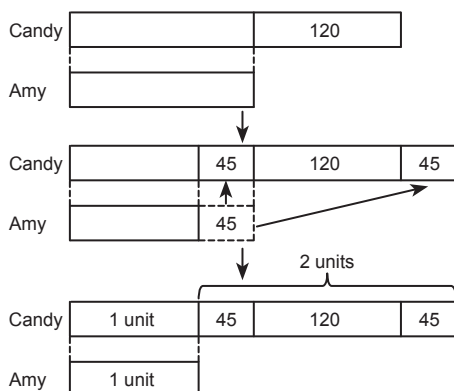
- 26 A A B C D A A A A B C D A A A ...  
 1 group  
 Number of letters in a group → 7  
 Number of groups of 7 letters →  $81 \div 7 = 11 \text{ R } 4$   
 Since the remainder is 4, the letter for the 81st position is the 4th position in a group → C

- 27 Average number of apples each boy received at first → 16  
 Average number of apples each boy received in the end → 10  
 Difference in average number of apples each boy received →  $16 - 10 = 6$   
 Number of rotten apples → 30  
 Number of boys →  $30 \div 6 = 5$

- 28 Fraction of red and white beads →  $1 - \frac{1}{8} = \frac{7}{8}$   
 Ratio of white beads to red beads → 2 : 3  
 Total number of units representing white and red beads  
 $\rightarrow 2 \text{ units} + 3 \text{ units} = 5 \text{ units}$   
 Fraction of white beads →  $\frac{2}{5} \times \frac{7}{8} = \frac{14}{40}$   
 Fraction of red beads →  $\frac{3}{5} \times \frac{7}{8} = \frac{21}{40}$   
 Fraction of blue beads →  $\frac{1}{8} (\times 5) = \frac{5}{40}$   
 Ratio of white beads to red beads to blues beads  
 $\rightarrow 14 : 21 : 5$

- 29 Number of stamps Leo collected → y  
 Number of stamps Tim collected  
 → twice as many stamps as Leo  
 $\rightarrow 2 \times y$   
 $= 2y$   
 Number of stamps Carl collected  
 $\rightarrow \frac{2}{3}$  as many as Tim  
 $\rightarrow \frac{2}{3} \times 2y$   
 $= \frac{4y}{3}$

- 30 Amy had 120 fewer stamps than Candy at first which means Candy had 120 more stamps than Amy at first. Number of stamps Amy gave Candy → 45  
Number of stamps Candy had in the end → 3 times as many as Amy



$$2 \text{ units} = 45 + 120 + 45$$

$$= 210$$

$$1 \text{ unit} = 210 \div 2$$

$$= 105$$

Number of stamps Amy had at first  
→ 1 unit + 45  
= 105 + 45  
= **150**

#### Paper 2

- 1 Amount of money Terence paid for 4 chairs with 7% GST → \$417.30

$$107\% \rightarrow \$417.30$$

$$1\% \rightarrow \$417.30 \div 107 = \$3.90$$

$$\text{GST} \rightarrow 7\% \rightarrow \$3.90 \times 7 = \$27.30$$

Discounted price of 4 chairs without GST

$$\rightarrow \$417.30 - \$27.30 = \$390$$

Percentage discount → 25%

$$\text{Percentage after discount} \rightarrow 100\% - 25\% = 75\%$$

$$75\% \rightarrow \$390$$

$$100\% \rightarrow \frac{100}{75} \times \$390 = \$520$$

Original cost of 4 chairs → \$520

$$\text{Original cost of 1 chair} \rightarrow \$520 \div 4 = \$130$$

**Alternative method:**

With discount

$$1 \text{ chair} \rightarrow \$417.30 \div 4$$

$$= \$104.325 \text{ (107\% of discounted price of 1 chair)}$$

Discounted price

$$\text{w/o GST} \rightarrow \$104.325 \times \frac{100\%}{107\%} = \$97.50$$

Before discount

$$75\% \text{ of original price} \rightarrow \$97.50$$

$$100\% \text{ of original price of 1 chair} \rightarrow \frac{100\%}{75\%} = \mathbf{\$130}$$

The cost of each chair before the discount without the GST was **\$130**.

- 2 Number of bags of marbles sold on Monday → 120  
Number of bags of marbles sold on Tuesday → 150  
Difference in number of bags of marbles sold on Monday and on Tuesday → 150 - 120 = 30  
Percentage increase →  $\frac{30}{120} \times 100\% = \mathbf{25\%}$

- 3 Fraction of red pens Rose bought →  $\frac{3}{7}$  (3 units)

$$\text{Fraction of blue pens Rose bought} \rightarrow 1 - \frac{3}{7}$$

$$= \frac{4}{7} \text{ (4 units)}$$

Difference in number of units representing red and blue

pens Rose bought → 4 units - 3 units = 1 unit

Number of blue pens Rose bought

→ 18 more than red pens

$$1 \text{ unit} = 18$$

Total number of pens Rose bought → 18 × 7 units

$$= 126$$

$$\text{Fraction of blue pens Jason bought} \rightarrow \frac{3}{5} \text{ (3 units)}$$

$$\text{Fraction of red pens Jason bought} \rightarrow 1 - \frac{3}{5}$$

$$= \frac{2}{5} \text{ (2 units)}$$

Total number of pens Jason bought

→ 59 more than Rose

$$\rightarrow 59 + 126$$

$$= 185$$

$$5 \text{ units} = 185$$

$$1 \text{ unit} = 185 \div 5 = 37$$

Number of red pens Jason bought → 37 × 2

$$= 74$$

Jason bought **74** red pens.

- 4 Fraction of flour Eunice used in 8 days

$$\rightarrow \frac{3 \times 8}{5 \times 8}$$

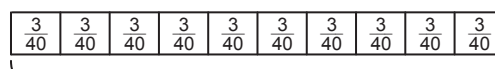
$$= \frac{24}{40} \text{ (24 units)}$$

Fraction of flour Eunice used in 1 day →  $\frac{3}{5} \div 8$

$$= \frac{3}{5} \div 8$$

$$= \frac{3}{5} \times \frac{1}{8}$$

$$= \frac{3}{40}$$



Fraction of flour Eunice used in 10 days →  $\frac{3}{40} \times 10$

$$= \frac{3}{4}$$

Fraction of flour Eunice left →  $1 - \frac{3}{4}$

$$= \frac{4}{4} - \frac{3}{4}$$

$$= \frac{1 \times 10}{4 \times 10}$$

$$= \frac{10}{40} \text{ (10 units)}$$

Mass of flour Eunice left → 120 g

$$10 \text{ units} = 120 \text{ g}$$

$$1 \text{ unit} = 120 \text{ g} \div 10$$

$$= 12 \text{ g}$$

$$24 \text{ units} = 12 \text{ g} \times 24$$

$$= 288$$

Eunice used **288 g** of flour during the first 8 days.

5 Before

vanilla : chocolate  
 20% : 80% (100% – 20%)  
 1 u : 4 u

After

vanilla : chocolate  
 36% : 64% (100% – 36%)  
 9 p : 16 p

$$\begin{aligned} 9p &= 1u + 100 \\ 16p &= 4u \\ 16 \times (1u + 100) &= 9 \times (4u) \\ 16u + 1600 &= 36u \\ 20u &= 1600 \\ 1u &= 80 \end{aligned}$$

Total cupcakes at first (5 u) =  $5 \times 80$   
 = **400**

6 Cindy collected 20% fewer stamps than Wendy.

Cindy : Wendy  
 100% – 20% = 80% : 100%  
 4 : 5

Cindy collected 40% more stamps than Doreen.

Cindy : Doreen  
 100% + 40% = 140% : 100%  
 7 : 5

Cindy : Wendy : Doreen  
 $4 \times 7$  :  $5 \times 7$   
 $7 \times 4$  :  $5 \times 4$   
 28 : 35 : 20

Number of stamps Cindy collected → 252

28 units = 252

1 unit =  $252 \div 28$   
 = 9

Number of stamps Doreen collected →  $9 \times 20$  units  
 = 180

Doreen collected **180** stamps.

7 To find the number of vanilla cupcakes, we have to assume all the amount of money was spent on the chocolate cupcakes first.

Cost of 57 chocolate cupcakes →  $\$2.80 \times 57$   
 = \$159.60

Difference with actual amount →  $\$169.60 - \$159.60$   
 = \$10

Difference in cost of 1 vanilla cupcake and 1 chocolate cupcake →  $\$3.20 - \$2.80 = \$0.40$

Number of vanilla cupcakes she bought →  $\$10 \div \$0.40$   
 = 25

Sophia bought **25** vanilla cupcakes.

8 Paul:

5 hours → 1 house

1 hour →  $\frac{1}{5}$  of the house

2 hours →  $\frac{1}{5} \times 2$  of the house

Paul can paint  $\frac{2}{5}$  of the house in 2 hours.

Dave:

6 hours → 1 house

1 hour →  $\frac{1}{6}$  of the house

2 hours →  $\frac{1}{6} \times 2$  of the house

Dave can paint  $\frac{2}{6}$  of the house in 2 hours.

Fraction of house painted by both in 2 hours

$$\begin{aligned} &\rightarrow \frac{2 \times 6}{5 \times 6} + \frac{2 \times 5}{6 \times 5} \\ &= \frac{12}{30} + \frac{10}{30} \\ &= \frac{22 \div 2}{30 \div 2} \\ &= \frac{11}{15} \end{aligned}$$

$\frac{11}{15}$  of the house would be painted by them in 2 hours.

9 (a)

Pattern	1st	2nd	3rd	4th	5th
Number of circles	7	10	13	16	19

$\begin{array}{ccccccc} & & \curvearrowright & & \curvearrowright & & \curvearrowright & & \curvearrowright & & \\ & & +3 & & +3 & & +3 & & +3 & & \end{array}$

(b) 999th pattern →  $7 + (998 \times 3)$   
 =  $7 + 2994$   
 = 3001

There will be **3001** circles in the 999th pattern.

10 Radius of small quarter →  $18 \text{ cm} \div 2 = 9 \text{ cm}$

Area of unshaded triangle →  $\frac{1}{2} \times \text{base} \times \text{height}$   
 →  $\frac{1}{2} \times 9 \text{ cm} \times 9 \text{ cm}$   
 = 40.5 cm<sup>2</sup>

Area of unshaded small quarter

$$\begin{aligned} &\rightarrow \frac{1}{4} \times \pi r^2 \\ &\rightarrow \frac{1}{4} \times 3.14 \times 9 \text{ cm} \times 9 \text{ cm} \\ &= 63.585 \text{ cm}^2 \end{aligned}$$

Area of big quarter circle

$$\begin{aligned} &\rightarrow \frac{1}{4} \times \pi r^2 \\ &\rightarrow \frac{1}{4} \times 3.14 \times 18 \text{ cm} \times 18 \text{ cm} \\ &= 254.34 \text{ cm}^2 \end{aligned}$$

Area of shaded part

$$\begin{aligned} &\rightarrow 254.34 \text{ cm}^2 - 40.5 \text{ cm}^2 - 63.585 \text{ cm}^2 \\ &= 150.255 \text{ cm}^2 \\ &\approx 150 \text{ cm}^2 \end{aligned}$$

The area of the shaded part is about **150 cm<sup>2</sup>**.

11 Ratio of number of apples, oranges and pears Kate bought → 3 : 2 : 5

Cost of an apple → \$0.80

Cost of an orange → \$1.00

Cost of a pear → \$1.20

Total amount of money spent → \$104

Number of units representing amount of money spent on apples →  $3 \text{ u} \times \$0.80 = 2.4 \text{ u}$

Number of units representing amount of money spent on oranges →  $2 \text{ u} \times \$1.00 = 2 \text{ u}$

Number of units representing amount of money spent on pears  $\rightarrow 5 u \times \$1.20 = 6 u$   
 Total number of units  $\rightarrow 2.4 u + 2 u + 6 u = 10.4 u$   
 $10.4 u = \$104$   
 $1 u = \$104 \div 10.4 = 10$   
 Number of oranges bought ( $2 u$ )  $\rightarrow 10 \times 2 = 20$   
 Number of pears bought ( $5 u$ )  $\rightarrow 10 \times 5 = 50$   
 Number of oranges and pears bought  $\rightarrow 20 + 50 = 70$   
 Kate bought **70** oranges and pears.

- 12 Amount Merri spent on headphones  $\rightarrow \$120$

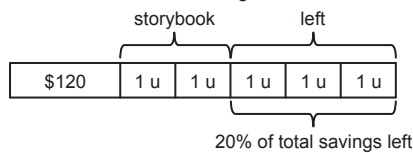
Fraction of savings spent on storybook

$\rightarrow 40\%$  of her remaining savings

$$= \frac{40}{100} \text{ of her remaining savings}$$

$$= \frac{2}{5} \text{ of her remaining savings}$$

Fraction of savings left  $\rightarrow \left(1 - \frac{2}{5}\right)$  of her remaining savings  
 $= \frac{3}{5}$  of her remaining savings



From the above model diagram,

$$3 u \rightarrow 20\%$$

$$5 u \rightarrow \frac{5}{3} \times 20\% = \frac{5}{3} \times \frac{20}{100} = \frac{1}{3}$$

Fraction of savings left and spent on storybook  $\rightarrow \frac{1}{3}$

Fraction of savings spent on headphones

$$\rightarrow 1 - \frac{1}{3} = \frac{2}{3} \text{ (2 units)}$$

$$2 \text{ units} = \$120$$

$$1 \text{ unit} = \$120 \div 2 = \$60$$

$$\text{Total savings at first} \rightarrow \$60 \times 3 \text{ units} = \$180$$

Merri had a savings of **\$180** at first.

- 13 Fraction of paper painted red  $\rightarrow \frac{2 \times 3}{5 \times 3} = \frac{6}{15}$

$$\text{Fraction of paper painted green} \rightarrow \frac{1 \times 5}{3 \times 5} = \frac{5}{15}$$

$$\text{Fraction of remaining space} \rightarrow 1 - \frac{6}{15} - \frac{5}{15} = \frac{4}{15}$$

Fraction of paper painted blue  $\rightarrow \frac{1}{2}$  of the remaining space

$$\rightarrow \frac{1}{2} \times \frac{4}{15}$$

$$= \frac{2}{15}$$

$$\text{Fraction of paper painted} \rightarrow \frac{6}{15} + \frac{5}{15} + \frac{2}{15}$$

$$= \frac{13}{15}$$

$$\text{Fraction of paper not painted} \rightarrow 1 - \frac{13}{15} = \frac{2}{15}$$

$$\text{Area of paper not painted} \rightarrow 240 \text{ cm}^2$$

$$2 \text{ units} = 240 \text{ cm}^2$$

$$1 \text{ unit} = 240 \text{ cm}^2 \div 2 = 120 \text{ cm}^2$$

$$\text{Area of whole paper} \rightarrow 120 \text{ cm}^2 \times 15 \text{ units} = 1800 \text{ cm}^2$$

Its length was twice its breadth.

Number of units representing area of rectangular paper  
 $\rightarrow 2 u \times 1 u = 2 u^2$

$$2 u^2 \rightarrow 1800 \text{ cm}^2$$

$$1 u^2 \rightarrow 1800 \text{ cm}^2 \div 2 = 900 \text{ cm}^2$$

$$1 u \times 1 u \rightarrow 1 u^2$$

$$30 \text{ cm} \times 30 \text{ cm} = 900 \text{ cm}^2$$

$$1 u \rightarrow 30 \text{ cm}$$

Length of rectangular paper  $\rightarrow 30 \text{ cm} \times 2 u = 60 \text{ cm}$

Breadth of rectangular paper  $\rightarrow 30 \text{ cm}$

Perimeter  $\rightarrow (60 \text{ cm} + 30 \text{ cm}) \times 2 = 180 \text{ cm}$

The perimeter of the paper was **180 cm**.

- 14 Volume of tank  $\rightarrow 50 \text{ cm} \times 30 \text{ cm} \times 20 \text{ cm}$   
 $= 30\,000 \text{ cm}^3$

$$\text{Volume of water in the tank} \rightarrow \frac{4}{15} \times 30\,000 \text{ cm}^3$$

$$= 8000 \text{ cm}^3$$

Volume of water needed to fill up the tank

$$\rightarrow 30\,000 \text{ cm}^3 - 8000 \text{ cm}^3 = 22\,000 \text{ cm}^3$$

Volume of water flowing from Tap A in 1 min

$$\rightarrow 0.5 \text{ l} = 500 \text{ ml}$$

Volume of water flowing from Tap A in 5 min

$$\rightarrow 500 \text{ ml} \times 5 = 2500 \text{ ml}$$

Since 3 l of water is poured from a container into the tank every 5 minutes,

at the 5th min

$$\rightarrow 2500 \text{ ml} + 3 \text{ l}$$

$$= 2500 \text{ ml} + 3000 \text{ ml}$$

$$= 5500 \text{ ml}$$

Every 5 minutes, 5500 ml of water would fill the tank.

Number of groups of 5 minutes to fill up the tank

$$\rightarrow 22\,000 \text{ cm}^3 \div 5500 \text{ ml}$$

$$= 4 \text{ groups}$$

Time taken to fill up the tank  $\rightarrow 4 \times 5 \text{ min}$

$$= 20 \text{ min}$$

It would take **20 min** to fill the tank to its brim.

- 15  $\frac{3}{3}$  of red balls +  $\frac{5}{5}$  of blue balls  $\rightarrow 270$

$$- \frac{1}{3} \text{ of red balls} + \frac{2}{5} \text{ of blue balls} \rightarrow 100$$

$$\frac{2}{3} \text{ of red balls} + \frac{3}{5} \text{ of blue balls} \rightarrow 170$$

$$- \frac{1}{3} \text{ of red balls} + \frac{2}{5} \text{ of blue balls} \rightarrow 100$$

$$\frac{1}{3} \text{ of red balls} + \frac{1}{5} \text{ of blue balls} \rightarrow 70$$

We need to eliminate red balls in order to find 1 unit of blue balls.

$$\frac{1}{3} \text{ of red balls} + \frac{2}{5} \text{ of blue balls} \rightarrow 100$$

$$- \frac{1}{3} \text{ of red balls} + \frac{1}{5} \text{ of blue balls} \rightarrow 70$$

$$0 \text{ red balls} + \frac{1}{5} \text{ of blue balls} \rightarrow 30$$

$$\frac{1}{5} \text{ of blue balls} \rightarrow 30$$

$$\frac{2}{5} \text{ of blue balls} \rightarrow 30 \times 2 = 60$$

Number of blue balls taken out  $\rightarrow 60$

Total number of balls taken out  $\rightarrow 100$

$$\text{Number of red balls taken out} \rightarrow 100 - 60$$

$$= 40$$

Michael took out **40** red balls.

**16 Initial ratio**

Singapore : Malaysia

$$40\% : 60\%$$

$$2 u : 3 u$$

In the end

$$\text{Singapore stamps} \rightarrow 2 u + 60$$

$$\begin{aligned} \text{Malaysia stamps} &\rightarrow \frac{50}{100} \times 3 u - 5 \\ &= 1.5 u - 5 \end{aligned}$$

Ratio in the end

Singapore : Malaysia

$$2 p : 1 p$$

This means that

Singapore stamps left = twice Malaysia stamps left

$$2 u + 60 = 2 \times (1.5 u - 5)$$

$$2 u + 60 = 3 u - 10$$

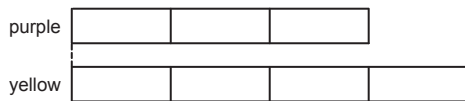
$$3 u - 2 u = 60 + 10$$

$$1 u = 70$$

$$\begin{aligned} \text{Stamps at first (5 u)} &\rightarrow 5 \times 70 \\ &= \mathbf{350} \end{aligned}$$

**17 Fraction of purple marbles  $\rightarrow \frac{3}{7}$  (3 units)**

$$\text{Fraction of yellow marbles} \rightarrow 1 - \frac{3}{7} = \frac{4}{7} \text{ (4 units)}$$



$\frac{17}{28}$  of the marbles were left in the box. This means that there were a total of 28 units of marbles. We have to divide each unit from the above model diagram to get a total of 28 units.

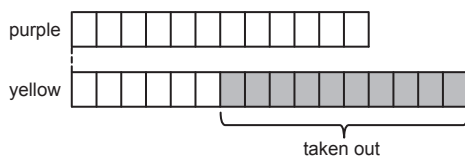
$$28 \div 7 \text{ units} = 4 \text{ smaller units for each unit}$$



$$\text{Fraction of yellow marbles taken out} \rightarrow \frac{5}{8}$$

Number of units representing yellow marbles taken out

$$\begin{aligned} &\rightarrow \frac{5}{8} \times 16 u \\ &= 10 u \end{aligned}$$



$\frac{17}{28}$  of the marbles were left in the box  $\rightarrow 17 u$  were left

Number of units representing yellow marbles left

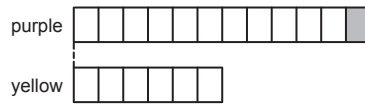
$$\begin{aligned} &\rightarrow 16 u - 10 u \\ &= 6 u \end{aligned}$$

Number of units representing purple marbles left

$$\begin{aligned} &\rightarrow 12 u - 6 u \\ &= 6 u \end{aligned}$$

Number of units representing purple marbles taken out

$$\begin{aligned} &\rightarrow 12 u - 11 u \\ &= 1 u \end{aligned}$$



Number of purple marbles taken out  $\rightarrow 20$

$$1 \text{ unit} = 20$$

$$\begin{aligned} \text{Number of marbles in the box at first} &\rightarrow 20 \times 28 \text{ units} \\ &= 560 \end{aligned}$$

There were **560** marbles in the box at first.